BRIEF COMMUNICATION

Electron Density Study of Garnets: Ca₃(Cr, Al)₂Si₃O₁₂

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The electron density distribution in a natural garnet, uvarovite Ca₃(Cr, Al)₂Si₃O₁₂ with 55% of the octahedral site occupied by Cr, has been studied with single-crystal X-ray diffraction methods through scattering factor refinement procedures. Electron density residuals up to 0.22 $e/Å^3$ in height indicating bonding electrons were detected between Si and oxygen. Characteristic aspherical electron density distribution around the (Cr, Al) site was also seen; six residuals, $-0.27 e/Å^3$ in height, are directed toward the coordinated oxygens, eight with 0.15 $e/Å^3$ height are directed away from the oxygens. [Cubic $Ia\bar{3}d$, a = 11.956(1)Å; Z = 8; $D_x = 3.734$ g/cm³; $F_{000} = 1897$; final R after anharmonic refinement: 0.0039 for 371 equivalent-averaged data.] © 1997 Academic Press

In view that garnets represent a structure type which has yet to be explored with present-day techniques for examining the electron density distribution in crystals, the crystal structure refinement of a natural silicate garnet, uvarovite $Ca_3(Cr, Al)_2Si_3O_{12}$, has been determined. A generalized formula for garnets $Z_3X_2T_3O_{12}$ with Z = Ca, X = Cr, etc., and T = Si will be used hereafter.

A natural specimen of the mineral uvarovite from the Ural mountains was rounded into a sphere of 0.16 mm diameter. The mean values of EPMA analyses for six points in the vicinity of the sample used showed the actual formula to be approximately $Ca_3(Cr_{1.10}Al_{0.80}, Ti_{0.06}, Fe_{0.03})Si_3O_{12}$ with scatter of 5% for Cr, 6% for Al, 19% for Ti, and 50% for Fe with one point below detection threshold. Cell dimensions were determined from the twenty-four equivalents of the 24 16 0 reflection ($2\theta = 117.65^{\circ}$) using MoK α_1 radiation (0.70926 Å) with a RIGAKU AFC5 automated fourcircle diffractometer (40 kV, 30 mA). Intensity data were collected with MoK α radiation (0.7017 Å); scan conditions, 2θ - ω mode, width $1.8 + 0.35 \tan \theta(^{\circ})$ in ω , speed $5^{\circ}/\text{min}$, up to 3 repeats until $|F_0| > 200\sigma(F_0)$. For a range |h|, |k|, $|l| \le 32, 2\theta \le 145^\circ, \sin \theta/\lambda \le 1.342, 20,845$ equivalent reflections were measured in full reciprocal space, which were generated from 537 independent data observed with $|F_0| > 6\sigma(F_0)$ from the 1530 measured in a preliminary run with the same scan conditions. Some high-angle reflections in geometrically blind regions could not be measured. Finally, 371 independent data with all measured equivalents observed with $|F_0| > 6\sigma(F_0)$ were averaged from 13,868 of these equivalents ($R_{int} = 0.0049$).

The crystal structure was refined with a modified version of the program RADY (1) applying Lp, absorption $\left[\mu(MoK\alpha) = 38.75/cm\right]$, and isotropic extinction corrections, using fully ionized scattering factors (2,3), and dispersion correction values (4). The scattering factor values for the X site were calculated from the EPMA results. Weights proportional to the theoretical number of equivalents for each reflection were allotted. Conventional leastsquares refinement with harmonic temperature factors gave R = 0.0096, $R_W = 0.0111$. Scattering factor refinement was executed under conditions identical to that described in (5,6). Minimum R was attained for harmonic scattering factor refinement after 11 repeated runs (R =0.0054, $R_{\rm W} = 0.0061$). Anharmonic refinement with Gram-Charlier series-expanded parameters up to sixth-rank tensors was run using the harmonically obtained scattering factors (symmetry restrictions taken from (7); R = 0.0040, $R_{\rm W} = 0.0044$). Four additional iterations of scattering factor refinement with anharmonic parameters resulted in $R = 0.0039, R_{\rm W} = 0.0042.^{1}$

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harmonic refinement / scattering factors refined



anharmonic refinement / scattering factors refined

FIG. 1. Difference Fourier sections (see Footnote 1) of a plane passing through the T, X, and O sites. Positive contours are shown in full, zero contours in broken, and negative contours in dotted lines with increments of 0.05 e/Å³. The map dimension is 3 × 5 Å. Residuals indicating bonding electrons are situated ~ 0.9 Å from the T site, toward 12 o'clock and 4 o'clock directions.

RESULTS AND DISCUSSION

Anharmonic refinement resulted in significantly shortened T-O distance, from 1.6463(3) Å for the harmonic to 1.6439(8) Å for the anharmonic scattering factor refinement (see Footnote 1).

Positive residuals situated between the T and O sites indicating bonding electrons are observed (Fig. 1; see also Footnote 1) with 0.22 $e/Å^3$ height for the harmonic and $0.11 \ e/\text{Å}^3$ height for the anharmonic scattering factor refinement. For the harmonic refinement, six residuals $-0.27 \ e/Å^3$ in height are arranged octahedrally around the X site approximately toward the oxygen atoms, while eight $0.15 e/Å^3$ height are arranged avoiding the oxygen atoms in the octahedral face directions. Similar arrangements of electron density residuals were seen around the Cr site in Cr_2O_3 (8) and $MgCr_2O_4$ (9), which are believed to indicate the aspherically deformed distribution of the d electrons.² There are no significant signs of the residual peak observed in the

gallium garnets (6) at Wyckoff position 48g (variable coordinate $y = \frac{1}{4}$, which was attributed to constructive interference of X-rays diffracted from domains with different structural motifs.

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²Conceivably, the peak heights of the residuals around the X site seen in the present work represent those of Cr occupying 55% of the X site. A pure substance would show higher peak heights accordingly.